
NAME (FIRST AND LAST): _____

UNI: _____

TIME IN: _____ TIME OUT: _____

INTEGRATION BEE QUALIFYING ROUND

DURATION: ONE HOUR

COLUMBIA UNIVERSITY

FEBRUARY 20, 2026

WRITE THE FINAL ANSWER IN THE SPACE PROVIDED. YOU HAVE ONE HOUR. NO CALCULATOR ALLOWED.

1. $\int \frac{x^3}{1+x^2} dx$ Answer: _____.

2. $\int \frac{\ln \sqrt{x}}{x^2} dx$ Answer: _____.

3. $\int_0^{\pi/2} x \sin x dx$ Answer: _____.

4. $\int_0^1 x^2 \ln(1+x) dx$ Answer: _____.

5. $\int \frac{\sqrt{1+x}}{x^2} dx$ Answer: _____.

6. $\int \frac{dx}{1+\sin x}$ Answer: _____.

7. $\int_0^{2\pi} \frac{\sin(2x)}{2+\cos x} dx$ Answer: _____.

8. $\int \frac{x^2}{x^6+9} dx$ Answer: _____.

9. $\int \frac{1}{\sin x - \cos x} dx$ Answer: _____.

10. $\int \ln(x + \sqrt{x^2 + 1}) dx$ Answer: _____.

11. $\int_0^1 \frac{\arctan x}{1+x} dx$ Answer: _____.

12. $\int \frac{dx}{\sqrt{1+\sin x}}$ Answer: _____.

13. $\int_0^1 \frac{\sqrt{x}}{\sqrt{2-x}} dx$ Answer: _____.

14. $\int \frac{dx}{x^2 + 2x \cos a + 1} \quad (a \in (0, \pi))$ Answer: _____.

15. $\int \frac{x^2 + 1}{x^4 + 1} dx$ Answer: _____.

16. $\int \frac{1}{\sqrt{x}} \ln\left(\frac{1+\sqrt{x}}{1-\sqrt{x}}\right) dx$ Answer: _____.

17. $\int_{-1}^1 \frac{\arctan x}{x^2 + 1} dx$ Answer: _____.

18. $\int_0^\infty \frac{e^{-x} - e^{-2x}}{x} dx$ Answer: _____.

19. $\int_0^1 \frac{x-1}{\ln x} dx$ Answer: _____.

20. $\int_0^{\pi/2} \frac{dx}{1 + (\tan x)^\pi}$ Answer: _____.

21. $\int \frac{x}{1+x+e^x} dx$ Answer: _____.

22. $\int (x+1)^2 e^{x-\frac{1}{x}} dx$ Answer: _____.

23. $\int_0^1 [nx]^2 dx \quad (n \in \mathbb{N})$ Answer: _____.

24. $\int_0^{\pi/2} \frac{\sin^{2026} x}{\cos^{2026} x + \sin^{2026} x} dx$ Answer: _____.